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## Active flow control of the airflow of a ship at yaw

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### ABSTRACT

This paper implements the steady Coanda effect active flow control (AFC) on the Chalmers ship model (CSM) to study its influence on the ship's side force and airwake under the yaw effect. The study is conducted numerically using Large Eddy Simulation (LES) with Wall-Adapting Local-Eddy Viscosity (WALE) model. Numerical methods are validated by the experimental data acquired from the baseline CSM under 10° port-side wind. The model with AFC is created by modifying the square-shaped hanger base to the Coanda surface and added with injection slots along the base's roof edge and two side edges. The results show that the base-shape modification significantly alters the vortex structure on deck from z-direction vortex (ZV) to streamwise vortex (SV), and the steady Coanda effect with a momentum coefficient ( $C_{\mu}$ ) of 0.02 further enhances the SV with the removal of port-side vortex (PV). The side force and yaw moment are reduced by 5.27% and 7.97%, respectively in the AFC case due to the reduction of port-side (windward) ship-surface pressure. Furthermore, the current AFC can suppress the low-speed region and alleviate the velocity gradient in the lateral direction, which mitigates the regions of high TKE (turbulent kinetic energy) and high shear stress along the port-side deck.

### 1. Introduction

Extensive studies have been conducted on the ship's air wake (Syms, 2008; Forrest and Owen, 2010; Herry et al., 2011; Kääriä et al., 2013; Gallas et al., 2017; Crozon et al., 2018; Shukla et al., 2021; Nisham et al., 2021) that is characterized by large unsteadiness, massive separation, and shear layer interactions. Under the yaw effect (cross-flow or wind-on-deck, WOD), the flow structure becomes even more complex (Rhoades and Healey, 1992; Zan, 2001) with enhanced unsteadiness. The ship's air wake, therefore, poses a serious challenge for helicopter recovery and launch, leading to significantly increased pilot's workload and safety issues (Forrest and Owen, 2010). A yaw effect also has negative influences on side forces, which reduces ships' stability and maneuverability. In this regard, flow control is expected to play a critical role in countering the above influences under the yaw effect.

Flow control can be categorized as passive flow control (PFC) that does not require external flow source, and active flow control (AFC) that does. Significant efforts to suppress the influence of yaw is made from the passive flow control perspective. Greenwell and Barrett (2006) experimentally tested the inclined screen flow-control structures with various inclined angles, blockages, and locations on the Simplified Frigate Shape (SFS). With a 30° cross-flow, it was found that the tested configurations have limited effect on mitigating downwash flow but can substantially lower turbulence levels. Various fence structures were

tested on the DDG-81 model by Findlay and Ghee (2006) to study their effectiveness in altering mean and fluctuating velocity in the vicinity of the deck region. The parameters of interest included type (solid or porous), angle, size, and location of the fence. It was suggested that the addition of the fence can improve the flow condition on deck by suppressing the mean momentum loss and turbulent intensity. However, these improvements became less significant under the yaw effect as the ship's air wake deviates from the flight deck. LaSalle (2013) placed a notched fence on the top and side of the hanger to modify ship airwake flow structures for more expansive helicopter flight envelopes. However, with 15° yaw, the fence structure was only capable of altering the shape and size of the re-circulation region but had a negligible effect on the turbulent kinetic energy and Reynolds shear stress. Various PFC techniques, including flap, ramp, and notch, were studied on a ship model in oblique wind-on-deck (WOD) conditions (Kaaria, 2012). The hanger notch configuration could reduce the RMS (root-mean-square) heave, pitch, and roll of landing helicopters by as much as 40%–45% during lateral translation and 30%–40% over the landing region. Similar studies were also conducted by Yongjie et al. (2019) who implemented ramp and notch on the side of a simplified LPD-17 ship model, and a remarkable reduction of RMS rotor moment was achieved by a side ramp in 15° WOD. Bardera et al. (2021) modified the hanger to a similar shape with the re-circulation bubble for an aerodynamically

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optimized geometry. The angled and elliptical hangers with roof and sides modified achieved the overall best performance considering the mitigation of unsteadiness, reduction of low-speed area, and loss of interior volume. The study found that the geometrical modifications of roof and side were particularly effective to suppress the low-velocity areas behind the hanger in a broad range of WOD.

For the active flow control, [Shafer and Ghee \(2005\)](#) applied steady injection on the hanger base of a scaled DDG-81 ship model. Quantified by the velocity standard deviation, the unsteadiness in the landing region at zero yaw angle was reduced by 6.6% with the injection velocity of 2.5% of the free-stream. As the yaw angle increased to  $20^\circ$ , the reduction of unsteadiness was increased to 8.3% with the same injection velocity.

Overall, the previous flow control studies on ships at a yaw mainly focus on the suppression of unsteadiness, recovery of flow momentum loss, and improvement of helicopter operations. However, little attention has been paid to studying the flow control's effect on side force, which is critical for a ship's stability and maneuverability under the yaw effect. Moreover, most of the previous studies utilize passive flow control methods, whereas limited efforts have been made using active flow control that is more flexible with a higher potential in control effectiveness. Recently, [Xu et al. \(2022\)](#) implemented the steady Coanda effect AFC at the hanger-roof edge of the Chalmers ship model (CSM) and achieved desirable control effectiveness, including drag reduction and turbulent suppression in high energy efficiency. The study was conducted under the zero-yaw effect.

The present work is extended from the previous study ([Xu et al., 2022](#)) by considering the yaw effect and by applying the steady Coanda effect not only on the hanger-roof but also along both side-edges (details will be shown in Section 2). The objectives are to study the influences of this AFC on the side force for improving the ship's maneuverability and its influences on the mean and fluctuating quantities in the wake flow for benefiting maritime helicopter operation. The current study is conducted numerically using Large Eddy Simulation (LES) with Wall-Adapting Local-Eddy Viscosity (WALE) subgrid model. Experimental testing is also conducted to validate the numerical methods. Apart from studying the control effectiveness of the steady Coanda effect, the mechanism of turbulent suppression is also understood via the current study. To the authors' knowledge, the steady Coanda AFC has not been studied on ships for controlling airflow under the yaw effect. The present work is to shed some light on this topic.

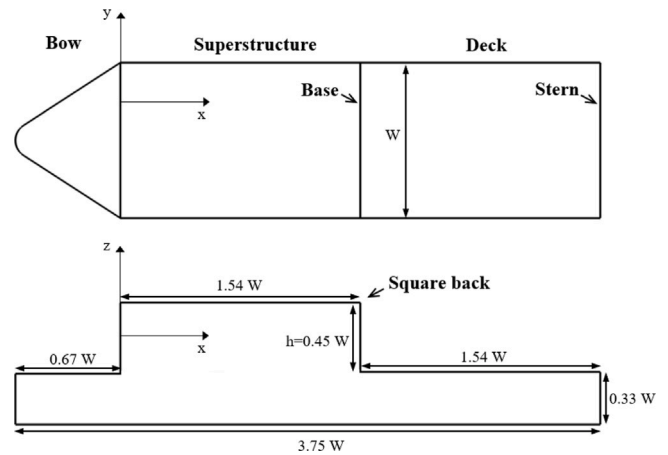
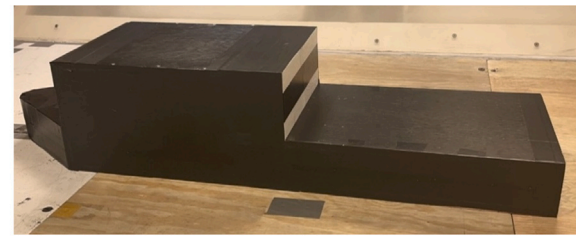
The remainder of the paper is organized as follows: Section 2 introduces the experimental setup, including wind tunnel facilities, test equipment, and test conditions; it also describes the numerical setup, including numerical methods, boundary conditions, and mesh resolutions. Section 3 starts with baseline validations followed by flow control results including the reduction of side force and yaw moment as well as the suppression of turbulent kinetic energy (TKE) and shear stress with the discussion of the suppression mechanism. Section 4 discusses three issues of applying the current AFC to a real ship.

## 2. Description of work

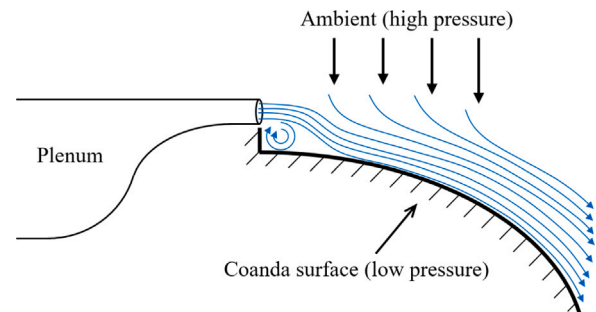
### 2.1. Experimental setup

This section describes the details of experiments with the ship model placed at the  $10^\circ$  yaw angle. The side force ( $F_y$ ), drag force ( $F_d$ ), and the distribution of pressure coefficients of the baseline Chalmers ship model (CSM) are measured experimentally, which are later used to validate the numerical methods. The present experimental setup is adopted from our previous work at zero-yaw condition ([Xu et al., 2022](#)).

The baseline CSM as shown on the top of [Fig. 1](#) is used in the present study that consists of a bow, hanger, base, deck, and stern. The width-to-height ratio ( $W/h$ ) of the hanger is 0.45 and is similar to that of the simplified ship model (SFS2 [Bardera and Meseguer, 2015](#)). Details



**Fig. 1.** The Chalmers ship model and its dimensions in top and side views.



**Fig. 2.** Illustration of the Coanda effect ([Xu et al., 2022](#)).

of model dimensions are shown in the middle and bottom of [Fig. 1](#). The width of the hanger ( $W$ ) is used as the characteristic length for normalization.

The Coanda effect is illustrated by the sketch in [Fig. 2](#), which is the tendency of a fluid jet to stay attached to a convex surface ([Tritton, 2012](#)). It is widely used for the active flow control on bluff bodies ([Freund and Mungal, 1994](#); [Barros et al., 2016](#); [Haffner et al., 2020](#)), ground vehicles ([Geropp and Odenthal, 2000](#); [Kee et al., 2001](#)), and airfoils ([Jones et al., 2002](#); [Sellars et al., 2002](#); [Jones, 2005](#); [Seele et al., 2013](#)).

The current flow control model shown in [Fig. 3](#) is modified based on the baseline CSM, which adds the injection slots near all edges (two sides and roof) of the base and modifies the square-back to a quarter-ellipse-shape Coanda surface. The ellipse shape is kept the same among sides and roof with a semi-major axis ( $a$ ) of  $20\%h$  and a semi-minor axis ( $b$ ) of  $15\%h$ , where  $h$  is the hanger height. The ellipse shape is selected over a circular shape due to a higher radius of curvature that has a better attachment and stronger Coanda effect of the jet flow. The ellipse shape and jet slot size are adopted from our previous study ([Xu et al., 2022](#)). The modified ship base, therefore, consists of three regions as shown in [Fig. 3](#): roof Coanda surface (green), sides

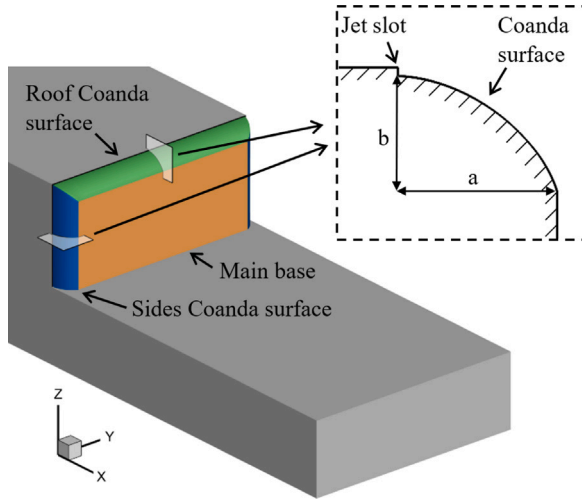


Fig. 3. Modification of Coanda surfaces and jet slots.

**Table 1**  
Locations of pressure probes ( $x/W$ ).

Numbers	1	2	3	4	5	6	7	8	9
Locations	0.08	0.14	0.24	0.54	0.73	0.92	1.10	1.25	1.38

Coanda surfaces (blue), and main base (orange). Modifying the square-back to the ellipse shape causes a volume loss of hanger by 0.4%.

The experiments on the baseline CSM are conducted in the closed-circuit L2 wind tunnel facilities at the Chalmers University of Technology as shown in Fig. 4. The closed test section of the wind tunnel has a cross-section of  $1.8 \text{ m} \times 1.25 \text{ m}$  with a length of 3 m. The blockage ratio of the baseline CSM in the test section is about 2.4%. The speed range of the wind tunnel is 0–60 m/s. The free-stream dynamic pressure and velocity are measured by the pitot tube placed at the beginning of the test section as shown in Fig. 4(a) and (c). The baseline CSM is tested at 5 m/s, which yields a Reynolds number ( $Re$ ) of  $8 \times 10^4$  based on the ship width. As illustrated in Fig. 4(a), the ship model is mounted on a six-component strain-gauge balance from RUAG of type 196-6H that is positioned underneath the tunnel floor. During testing, the ship model is exposed to a  $10^\circ$  port-side wind. This is achieved by rotating the force balance together with the ship model to the starboard (opposite) side as shown in Fig. 4(c). The side force ( $F_y$ ) and drag force ( $F_d$ ) acquired by the force balance is an averaged value for 20 s. The side force ( $C_y$ ) and drag coefficient ( $C_d$ ) are the normalization of  $F_y$  and  $F_d$  using Eqs. (1) and (2), respectively.

$$C_d = \frac{F_d}{0.5\rho_\infty u_\infty^2 A_s} \quad (1)$$

$$C_y = \frac{F_y}{0.5\rho_\infty u_\infty^2 A_s} \quad (2)$$

where  $\rho_\infty$  and  $u_\infty$  are the free-stream density and velocity,  $A_s$  is the ship cross sectional area at the zero-yaw position.

The pressure measurements are conducted using the differential pressure scanner 9116 with a scanning frequency of 62.5 Hz and a sampling time of 120 s. The pressure scanner is connected to the pressure probes using one-meter-long PVC tubes. The pressure distribution is obtained by the pressure probes located along the center of the deck as shown in Fig. 4(b). Table 1 presents the specific positions of probes relative to the base.

The pressure coefficient is obtained based on the measured pressure,

$$C_p = \frac{p - p_\infty}{0.5\rho_\infty u_\infty^2} \quad (3)$$

where  $p$  is the measured deck pressure,  $p_\infty$  is the free-stream pressure.

## 2.2. Numerical setup

This section describes the numerical setup of the present study. Large Eddy Simulation (LES) is conducted using the commercial finite volume software, Star-CCM+. The governing equations are the incompressible, spatially filtered 3D Navier–Stokes equations as shown in Eq. (4)–(6). The filter width,  $\Delta$ , is associated with the cell size and is defined as  $\Delta = (\Delta_i \Delta_j \Delta_k)^{1/3}$ .

$$\nabla \cdot (\rho \tilde{\mathbf{v}}) = 0 \quad (4)$$

$$\frac{\partial}{\partial t} (\rho \tilde{\mathbf{v}}) + \nabla \cdot (\rho \tilde{\mathbf{v}} \otimes \tilde{\mathbf{v}}) = -\nabla \cdot \tilde{\mathbf{p}} \mathbf{I} + \nabla \cdot (\tilde{\mathbf{T}} + \mathbf{T}_{SGS}) + \mathbf{f}_b \quad (5)$$

$$\frac{\partial}{\partial t} (\rho \tilde{\mathbf{E}}) + \nabla \cdot (\rho \tilde{\mathbf{E}} \tilde{\mathbf{v}}) = -\nabla \cdot \tilde{\mathbf{p}} \tilde{\mathbf{v}} + \nabla \cdot (\tilde{\mathbf{T}} + \mathbf{T}_{SGS}) \tilde{\mathbf{v}} - \nabla \cdot \tilde{\mathbf{q}} + \mathbf{f}_b \tilde{\mathbf{v}} \quad (6)$$

where  $\rho$  is the constant density,  $\tilde{\mathbf{v}}$  is the filtered velocity,  $\tilde{\mathbf{p}}$  is the filtered pressure,  $\mathbf{I}$  is the identity tensor,  $\tilde{\mathbf{T}}$  is the filtered stress tensor,  $\mathbf{f}_b$  is the resultant of the body forces,  $\tilde{\mathbf{E}}$  is the filtered total energy, and  $\tilde{\mathbf{q}}$  is the filtered heat flux.

The subgrid scale stress tensor  $\mathbf{T}_{SGS}$  is given in Eq. (7),

$$\mathbf{T}_{SGS} = 2\mu_t \tilde{\mathbf{S}} - \frac{2}{3}(\mu_t \nabla \cdot \tilde{\mathbf{v}}) \mathbf{I} \quad (7)$$

where  $\tilde{\mathbf{S}}$  is the strain rate tensor and  $\mu_t$  is the subgrid scale viscosity.

The Wall-Adapting Local-Eddy Viscosity (WALE) model proposed by Nicoud and Ducros (1999) is employed in the present study to provide the subgrid scale viscosity ( $\mu_t$ ) in the Boussinesq approximation of the subgrid-scale stress tensor. The WALE model has been validated in our previous numerical study on the same ship model (Xu et al., 2022, 2023). It is also extensively validated on predicting flows around the hatch back (Aljure et al., 2014) and the square back (Dalla Longa et al., 2019) Ahmed bodies that represent the bluff-body shape of the current ship model. The WALE model is, therefore, suitable for the current numerical study.

The WALE model computes the subgrid eddy viscosity based on the invariants of the velocity gradient and accounts for rotational rate. It is defined as

$$\mu_t = \rho(C_w \Delta)^2 \frac{(S_{ij}^* S_{ij}^*)^{3/2}}{(\tilde{S}_{ij}^* \tilde{S}_{ij}^*)^{5/2} + (S_{ij}^* S_{ij}^*)^{5/4}} \quad (8)$$

where the model coefficient  $C_w$  is 0.544.  $\tilde{S}$  is the strain rate tensor computed from the resolved velocity field.  $S_{ij}^*$  is the traceless symmetric part of the square of the velocity gradient tensor, defined as

$$S_{ij}^* = \frac{1}{2}(\tilde{g}_{ij}^2 + \tilde{g}_{ji}^2) - \frac{1}{3}\delta_{ij}\tilde{g}_{kk}^2 \quad (9)$$

where  $\delta_{ij}$  is the Kronecker delta and  $\tilde{g}_{ij} = \partial u_i / \partial x_j$ .

The convective flux is evaluated by a bounded central-differencing scheme that blends 98% of the 2nd-order central differencing scheme and 2% of the first-order upwind scheme for robustness purposes. The implicit unsteady solver with 2nd-order Euler implicit scheme is used to approximate the transient term. The physical time step ( $\Delta t$ ) is set to  $1.44 \times 10^{-4}$  s, which ensures that the CFL (Courant Friedrichs Lewy) number lower than 1 in over 99% cells. LES simulation starts from the preliminary flow field that is provided by a URANS simulation with  $k - \omega$  SST turbulence model. After a characteristic time ( $t^* = tU_\infty/h$ ) of 65 when all the aerodynamic forces become dynamically stable, the LES simulation begins sampling and averaging results for a  $t^*$  of 129.

Fig. 5 shows the computational domain with a cross-sectional area of  $6.5W \times 5W$ , which accounts for a blockage ratio of about 2.4%. The length of the domain is  $28W$  with  $8W$  from inlet to bow tip-point and  $16W$  from stern to outlet. The ship model sits on the floor with no gap in between. The coordinates system and velocity direction are denoted by  $x$  and  $u$  in the streamwise direction,  $y$  and  $v$  in the lateral (spanwise)

**Table 2**  
Results of the grid independent study.

Cases	Max $y^+$	Max $\Delta s^+$	Max $\Delta l^+$	No. of cells	$C_d$	$\Delta C_d$	$C_y$	$\Delta C_y$
Initial	< 1	< 55	< 21	$3.7 \times 10^7$	0.722	–	0.579	
Coarse	< 1	< 65	< 30	$2.6 \times 10^7$	0.718	–0.55%	0.577	–0.35%
Refined	< 1	< 40	< 15	$4.7 \times 10^7$	0.720	–0.28%	0.578	–0.17%

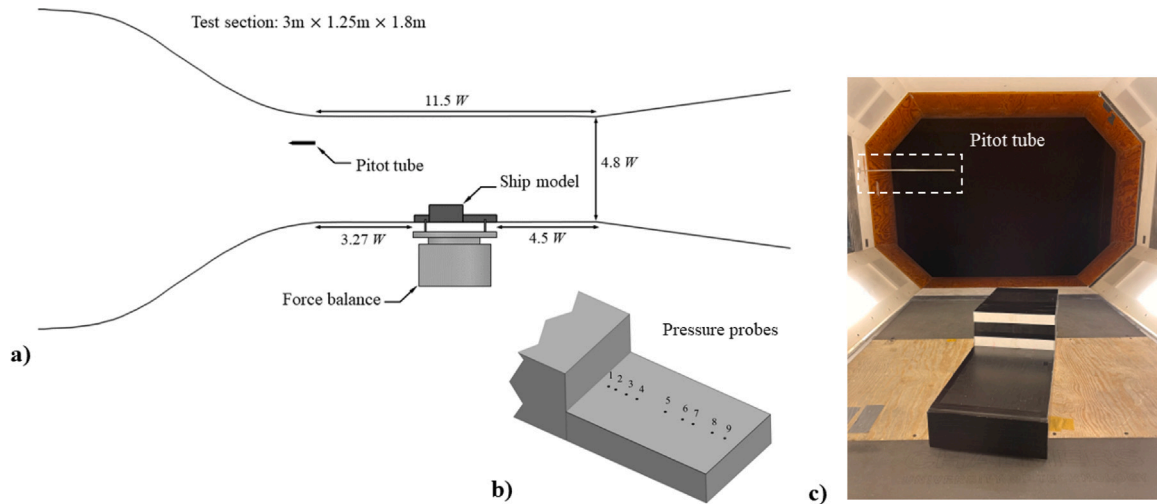


Fig. 4. Illustrations of the experimental setup: (a) schematics of Chalmers L2 wind tunnel, (b) locations of pressure probes on deck, (c) the Chalmers ship model placed in L2 wind tunnel with 10° yaw angle.

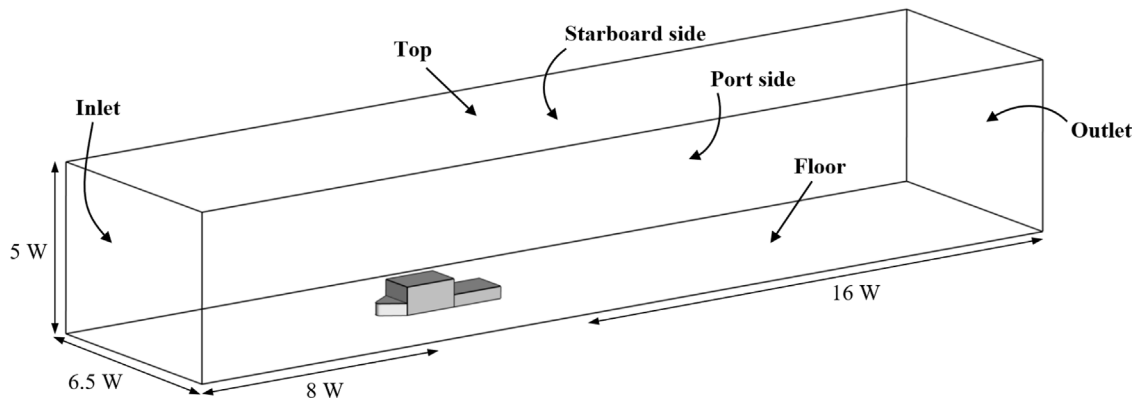


Fig. 5. Computational domain.

direction, and  $z$  and  $w$  in the vertical direction. As shown in Fig. 6, the free-stream  $u_\infty$  is added with a lateral component  $v_\infty$  to produce a 10° port-side wind  $U_p$ . The velocity inflow boundary condition with a uniform velocity  $U_p$  is specified at the inlet and port side of the computational domain shown in Fig. 5. Static pressure outlet boundary condition is applied at the outlet and the starboard side. The present setup of the inlet and outlet boundary conditions are adopted from the previous yaw-effect study on ships (Zhang et al., 2021). The top of the domain is specified with a symmetry boundary condition. The no-slip wall boundary condition is applied on the floor and all ship surfaces. For the cases with flow control, the velocity inlet boundary condition is specified at the injection exit without the injection duct simulated.

The structured hexahedral mesh is created using Pointwise. Fig. 7 shows the details of the mesh topology. The overall mesh size contains 37 million cells for the baseline model and 42 million cells for the model with flow control. The near-wall grid distance  $\Delta y$  is  $3 \times 10^{-5}$ , which ensures  $y^+ = \frac{\Delta y u_\tau}{\nu}$  lower than 1. For the resolution in streamwise ( $\Delta s^+ = \frac{\Delta s u_\tau}{\nu}$ ) and spanwise ( $\Delta l^+ = \frac{\Delta l u_\tau}{\nu}$ ) directions,  $\Delta s^+$  is less than 55 and the maximum  $\Delta l^+$  is 21, which satisfies the suggested ranges

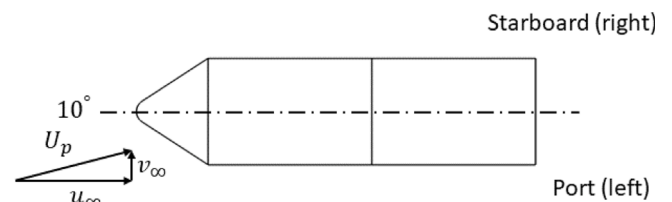


Fig. 6. 2D sketch of port-side free-stream  $U_p$ .

proposed by Piomelli and Chasnov (1996). Furthermore, as shown in Table 2, a grid dependency study is conducted based on a coarse mesh of 27 million cells and a refined mesh of 47 million cells. The acquired drag coefficients ( $C_d$ ) and side force coefficients ( $C_y$ ) fall in a very close range with those acquired from the initial mesh of 37 million cells. The deviation of  $\Delta C_d$  is less than 0.6%, and  $\Delta C_y$  is less than 0.3%. It also shows that both  $C_d$  and  $C_y$  acquired by the initial mesh are more

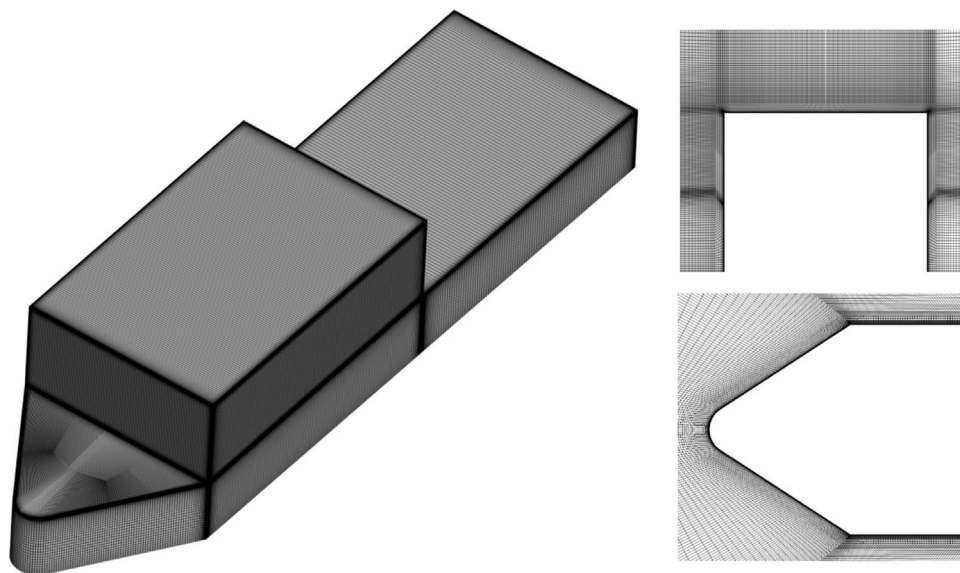


Fig. 7. Mesh topology of the Chalmers ship model (Xu et al., 2022).

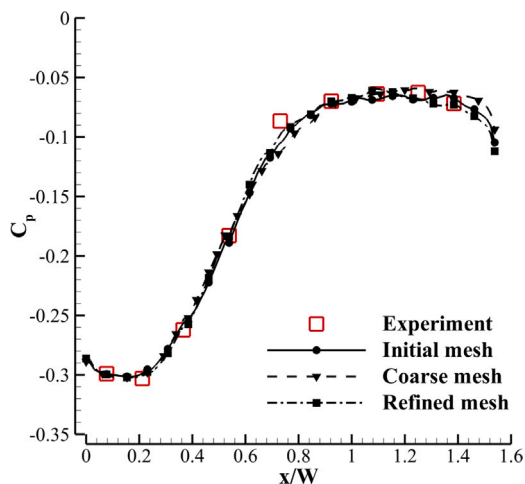


Fig. 8. The time-averaged  $C_p$  distribution at the center of deck.

consistence with the refined mesh, which suggests the convergence of solutions to the refined mesh. Note that the predicted drag and side forces are acquired by integrating the surface pressure and wall shear stress in  $x$  and  $y$  directions, respectively.

### 3. Results and discussions

#### 3.1. Baseline validation

The numerical method is validated by comparing the  $C_d$ ,  $C_y$ , and  $C_p$  distributions with the experimental measurements conducted under  $10^\circ$  yaw effect.

Table 3 compares the predicted  $C_d$  and  $C_y$  with the measured ones, where  $\Delta C_d$  and  $\Delta C_y$  indicate the deviations from the experiment. The drag coefficient  $C_d$  is 4.1% deviated from the experiment, and the side force coefficient  $C_y$  is 1.53% off.

Then, the  $C_p$  distribution along the center of the deck (Fig. 4(b)) is used for further validation. Fig. 8 shows that the predicted and measured  $C_p$  distributions are in a good agreement from base ( $x/W = 0$ ) to deck-end ( $x/W = 1.54$ ). Fig. 8 also shows that the predicted  $C_p$  distributions acquired by the three meshes virtually overlap with just

Table 3  
Predicted and measured  $C_d$  and  $C_y$ .

Cases	$C_d$	$\Delta C_d$	$C_y$	$\Delta C_y$
Experiment	0.753	-	0.588	-
CFD	0.722	-4.10%	0.579	-1.53%

a slightly higher deviation observed in the coarse mesh at  $x/W$  from 1.2 to 1.6. Overall, it is indicated that the current numerical method is capable of predicting the flow around the CSM with satisfactory accuracy, and the grid independence is achieved with the initial mesh size of 37 million cells.

#### 3.2. Numerical results of the baseline and flow control cases

This section presents the results of the controlled ship airflow under  $10^\circ$  yaw. Three cases are compared here, labeled as Cases 1–3: the baseline ship with square-back base, the modified ship base with roof and sides Coanda surfaces but no jet blowing, and the active flow control (AFC) case with jet blowing from both roof and two-sides slots. The AFC Case 3 has the total momentum coefficient  $C_\mu$  of 0.02 with 0.0125 from the roof slot and 0.0075 from the side-slots.

The momentum coefficient  $C_\mu$  is defined as

$$C_\mu = \frac{\dot{m}_j U_j}{0.5 \rho_\infty u_\infty^2 A_s} \quad (10)$$

where  $\dot{m}_j$  and  $U_j$  are the mass flow rate and velocity of the jet, respectively.

The flow structures of the three cases in the vicinity of the deck are illustrated in Fig. 9 using the 3D streamlines extracted from the time-averaged flow fields colored by the time-averaged  $u$  with the distribution of vortex cores marked by white lines. The 2D surface streamlines at the  $z$ -plane on the mid-hanger-height are also shown in the last column in Fig. 9. The pressure distribution at the base is colored by the time-averaged gauge pressure with a unit of [Pa]. Under the  $10^\circ$  port wind, significant yaw effects are manifested in the flow fields on deck. As shown in Fig. 9 (a), a re-circulation region with a  $z$ -direction vortex (ZV) can be observed at the starboard side downstream the base, which is substantially different from the horseshoe vortex structure (Shafer and Ghee, 2005) observed in zero-yaw cases. Such a ZV is caused by re-circulating the flow from starboard and hence, the base pressure is reduced due to the low-pressure vortex core. The

starboard flow also travels across the deck, however, blocked by the high-speed port-side flow and recirculates backwards and downstream as shown in Fig. 9 (b). Consequently, a low-speed region demonstrated by the iso-surface of  $u = 0$  m/s and a port-side vortex (PV) are induced. With the sharp edges of the base rounded to Coanda surfaces in Case 2, leeward flow attaches on the starboard base as shown in Fig. 9 (d), (e), and (f). As a result, the low-speed region (iso-surface of  $u = 0$  m/s) is suppressed and the z-direction vortex (ZV) observed in Case 1 is replaced by a streamwise vortex (SV) observed at the top-starboard corner of the base that is caused by the leeward flow interacting with the flow passing the roof Coanda surface. The SV has its core bounded on the base, which further reduces the base pressure. Similar to Case 1, the starboard flow in Case 2 travels across the deck but is blocked by the port-side flow, which also forms the port-side vortex (PV). With a  $C_\mu$  of 0.02 applied in Case 3, the leeward flow and roof flow are energized at the near base region, which enhances the streamwise vortex in its core length and moves the vortex core towards the port. The low-speed region is further suppressed compared to Cases 1 and 2, which leads to the disappearance of the port-side vortex (PV). Due to the jet blowing, jet flow accelerates on the Coanda surfaces and reduces the surface pressure as can be observed on the sides and roof Coanda surfaces in Fig. 9(g) and (h).

Fig. 10 shows the instantaneous streamwise velocity ( $u_{ins}$ ) at the symmetric and mid-deck-height planes. The suppression of the low-speed region downstream the base due to jet blowing is confirmed by the instantaneous contours where the low-speed region is constrained closer to the deck (Fig. 10(c)) as well as more to the port-side (Fig. 10(f)).

Fig. 11 shows the time-averaged  $u$  contours with the 2D streamlines at the symmetric plane. Three flow re-circulation regions are observed, one in the front of ship due to the blockage of superstructure, one near the leading edge of the roof due to the flow separating from the sharp edge, and the last one in the downstream of the base that is well discussed previously.

Fig. 12 shows the low-pressure region using the iso-surfaces of gauge static pressure at  $-5$  and  $-4$  (Pa), together with the white lines that mark the positions of vortex cores. A bulk of low-pressure region is observed downstream of the base due to the z-direction vortex (ZV). The port-side vortex (PV) also causes a low-pressure region near the port. Case 2 shown in Fig. 12(b) has the low-pressure region start to grow in the streamwise direction along the streamwise vortex core (SV). As the streamwise vortex is enhanced by the steady Coanda effect in Case 3, the low-pressure region is more stretched with its distribution presenting a pronounced streamwise pattern.

To evaluate the potential influence of the steady Coanda effect on the ship's stability and maneuverability. The coefficient of side forces ( $C_y$ ) and yaw moments ( $M_y$ ) of the three cases are compared in Table 4. Values of  $\Delta C_y$  and  $\Delta M_y$  are the reductions of the averaged side force and yaw moment compared to the baseline Case 1. The reductions of the RMS (root-mean-square) of side force ( $C_y$ ) and yaw moment ( $M_y$ ) are indicated by  $\Delta\langle C_y \rangle$  and  $\Delta\langle M_y \rangle$ , respectively. The overall reduction of side force ( $\Delta C_y$ ) is broken down to the contributions from different parts of the ship model: port-side surface ( $\Delta C_{yp}$ ), starboard-side surface ( $\Delta C_{ys}$ ), and the rest ( $\Delta C_{yr}$ , including jet effects and forces on the surfaces of roof, deck, base, bow, and stern). The yaw moment is the z-direction moment calculated by multiplying the side force with the  $x$  distance to a pivot fixing at the ship bow-tip point. As presented in Table 4, the  $10^\circ$  port-wind can generate significant side force and yaw moment for all cases, among which Case 1 has the highest values. With the steady Coanda effect applied in Case 3, the  $C_y$  and  $M_y$  are reduced by 5.27% and 7.97%, respectively. Table 4 also shows that the major changes of side force come from the side parts with the reduced side force on the windward port side and enhanced on the leeward starboard side as shown by the values of  $\Delta C_{yp}$  and  $\Delta C_{ys}$ .

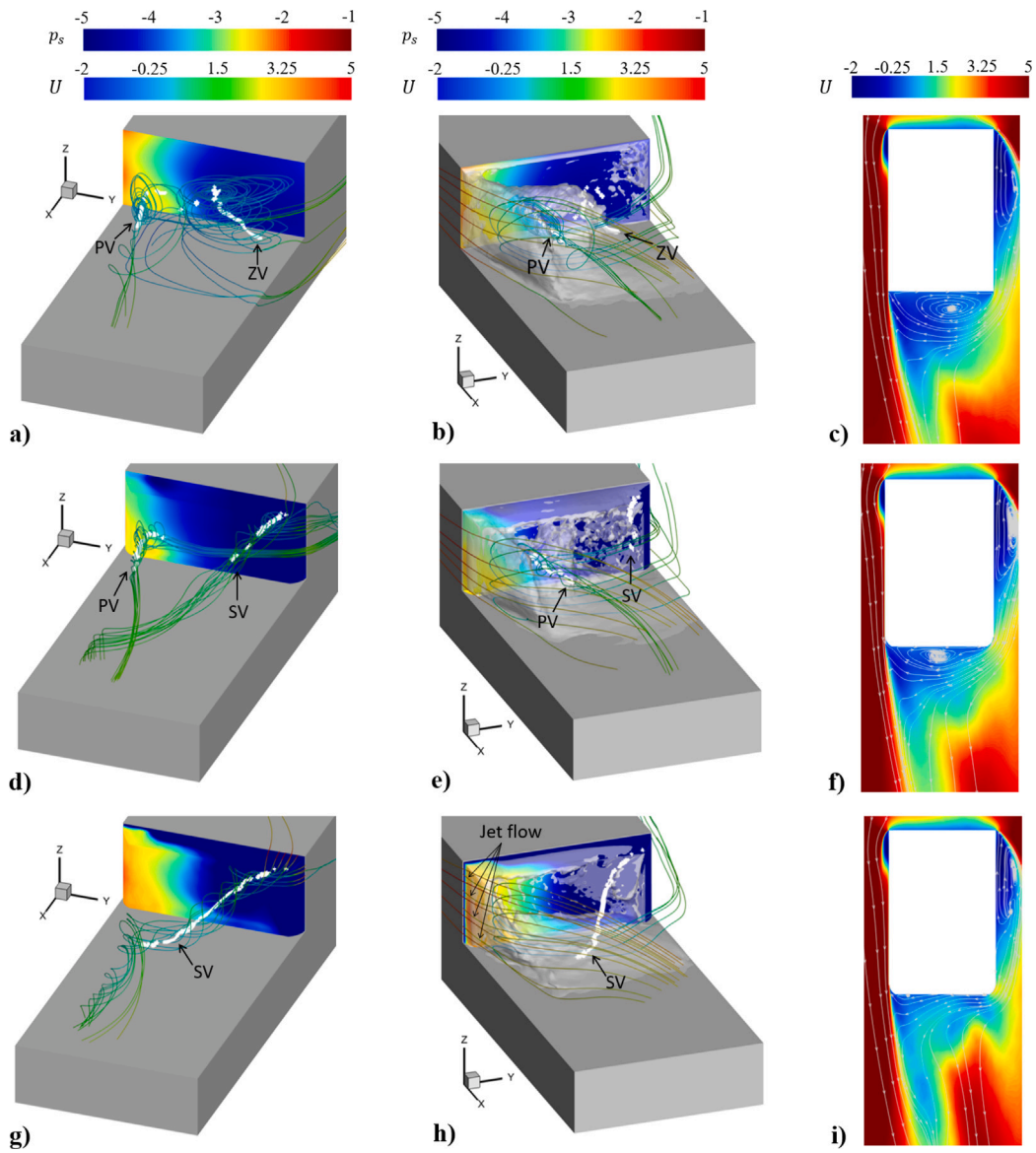
To explain the cause of side force variations, Figs. 13 and 14 show the time-averaged static pressure ( $p_s$ ) contours at starboard and port

sides of the ship model. On the starboard side as shown in Fig. 13, a similar pressure distribution is observed on the major part of the surface with the only difference occurring at the side-Coanda surface, which is due to pressure reduction from the Coanda effect and streamwise vortices as demonstrated in Figs. 9 and 12. Such surface-pressure reduction contributes to the increased starboard side force of  $\Delta C_{ys}$ . On the port, the pressure reduction is not only observed on the side-Coanda surface but also occupies more area in the upstream and downstream (enclosed by the dashed lines in Fig. 14(b) and (c)), which is the reason of the reduced  $\Delta C_{yp}$ . For further explanation, Fig. 15 plots the  $u$  profiles perpendicular to the port-side surface at the three interested stations marked in Fig. 14. The  $D/W$  in Fig. 15 is the normalized distance from surfaces. It is observed that the near-surface velocity in all stations is increased in Cases 2 and 3 as compared to Case 1, which increases the dynamic pressure and therefore achieves the reduced static pressure on the port-side surface. Furthermore, Fig. 15 shows that the velocity increment is gradually enhanced as the flow approaches the side-Coanda surface, and the highest increment is achieved by Case 3 with jet blowing. This suggests an explanation for the increased near-surface velocity that the low pressure region in the vicinity of the side-Coanda surface appears to create a suction effect, which induces the upstream flow, leading to the velocity increment. The downstream static pressure is also affected as the upstream flow with increased velocity reaches the downstream. Overall, both sides of the ship model has pressure decreased with flow control applied; nevertheless the port side (windward) has a more enhanced pressure reduction, which results in the mitigation of the overall side force.

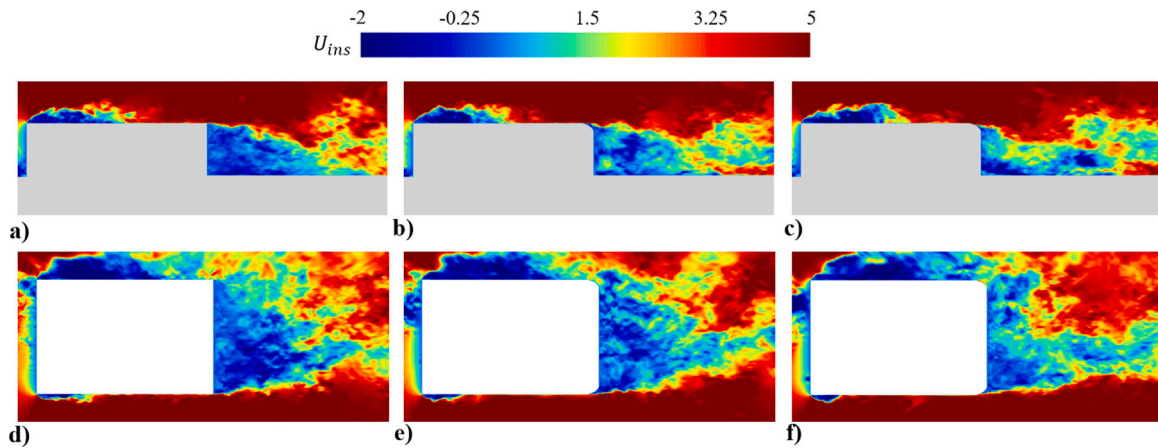
One of the important mean quantities is the streamwise velocity  $u$  on the ship deck. A higher incoming  $u$  velocity enables a helicopter takes off at a higher gross weight (Shafer and Ghee, 2005). Fig. 16 shows the time-averaged  $u$  contours at the three interested stations of  $x/W = 0.2, 0.8,$  and  $1.35$ , where  $W$  is the width of deck, and  $x/W = 0$  means the location of the hanger base. A low-speed region is observed at Station 1 in all cases, among which Case 3 with jet flow activated, have a significantly reduced size. The low-speed regions are reduced at both the port and starboard sides but has less reduction at port due to the re-circulation created by the cross-deck flow meeting with port main-flow as addressed previously with Fig. 9(b), (e), and (h).

During the recovery (landing) of a maritime helicopter, the turbulent fluctuation is one of the key factors that increases pilots' workload. The concerned region of turbulent fluctuation will depend on the selected recovery procedure. Here, we confine our interest to the Royal Navy's standard port-side forward-facing recovery (Roper et al., 2006), which is one of the most common routines. During the recovery as shown in Fig. 17, the helicopter approaches the deck hovering along the port-side deck and then performs a sidestep landing crossing the port-deck edge. In this regard, the turbulent fluctuation along the port-side deck plays a critical role in recovery efficiency.

To demonstrate the influence of the current AFC on the turbulent fluctuations at the concerned region, the turbulent kinetic energy (TKE), defined as  $0.5(\overline{u'u'} + \overline{v'v'} + \overline{w'w'})$  is used here for discussion. Note that TKE is normalized by the square of the free-stream velocity ( $u_\infty^2$ ). Fig. 18 shows the contours of TKE at three streamwise stations with the front view of Station 2 (mid-deck) for a better comparison. The starboard TKE at close-base Station 1 is increased in Case 3 but is quickly dissipated in the downstream Stations 2 and 3. As addressed previously, the port-side TKE is of more interest in helicopter recovery. It can be observed that the port-side TKE is suppressed in Case 3 for all stations. This is especially clear as demonstrated by the front views in the second row of Fig. 18. The high TKE region at the port side of Case 3 is smaller compared to the rest cases. Furthermore, Fig. 19 shows the high-shear-stress region along the port side using the iso-surface at  $\overline{u'v'} = 0.03$  (normalized by  $u_\infty^2$ ). Again, Case 3 achieves a largely mitigated shear-stress region as compared to Cases 1 and 2. The reduced TKE and  $\overline{u'v'}$  will benefit a helicopter recovery under the yaw effect.



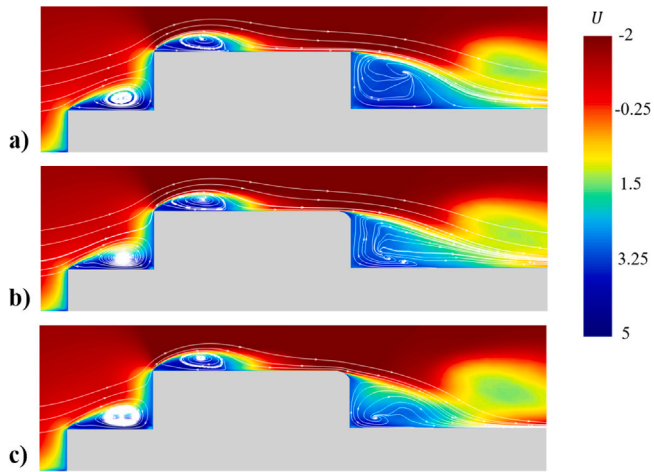
**Fig. 9.** The time-averaged static pressure distributions at the base and flow structures of the three cases: (a) (b) (c) Case 1, (d) (e) (f) Case 2, (g) (h) (i) Case 3; Column a-d-g is the starboard view showing the vortex cores and 3D streamlines colored by the time-averaged  $u$ ; Column b-e-h is the port view showing cross deck flows and low speed zone of iso-surface with  $u = 0$ ; Column c-f-i is the top view of 2D streamlines and the time-averaged  $u$  contours.



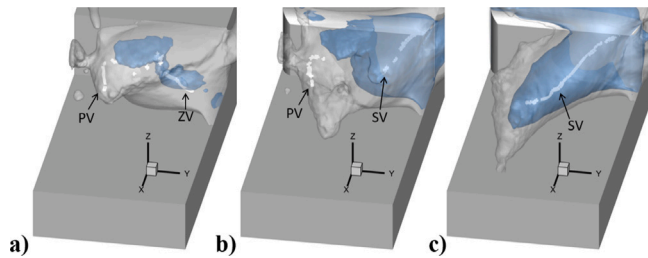
**Fig. 10.** The instantaneous streamwise velocity ( $u_{ins}$ ) contours at the symmetric ( $y = 0$ ) and mid-deck-height ( $z$ ) planes: (a) (d) Case 1, (b) (e) Case 2, (c) (f) Case 3; Row a-b-c shows the contours at plane  $y = 0$ ; Row d-e-f shows the contours at mid-deck-height  $z$  plane.

**Table 4**  
Comparisons of the time-averaged side force coefficients and yaw moments.

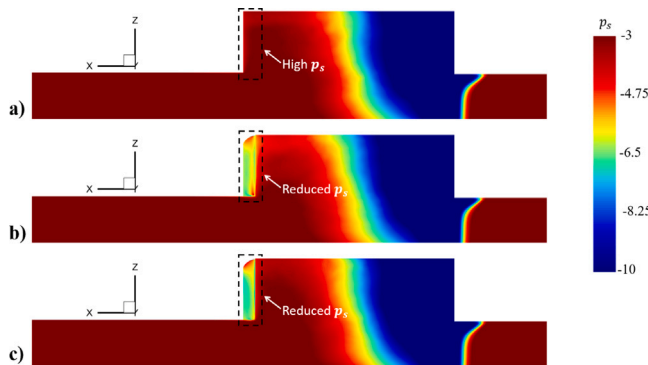
Cases	$C_y$	$M_y$	$\Delta C_{yp}$	$\Delta C_{yx}$	$\Delta C_{yr}$	$\Delta C_y$	$\Delta M_y$	$\Delta(C_y)$	$\Delta(M_y)$
Case 1	0.588	0.138	–	–	–	–	–	–	–
Case 2	0.567	0.130	–8.24%	4.61%	0.06%	–3.57%	–5.80%	–3.20%	–5.58%
Case 3	0.557	0.127	–11.68%	6.22%	0.19%	–5.27%	–7.97%	–4.95%	–7.46%



**Fig. 11.** The time-averaged  $u$  contours with 2D streamlines at the symmetric plane: (a) Case 1, (b) Case 2, (c) Case 3.

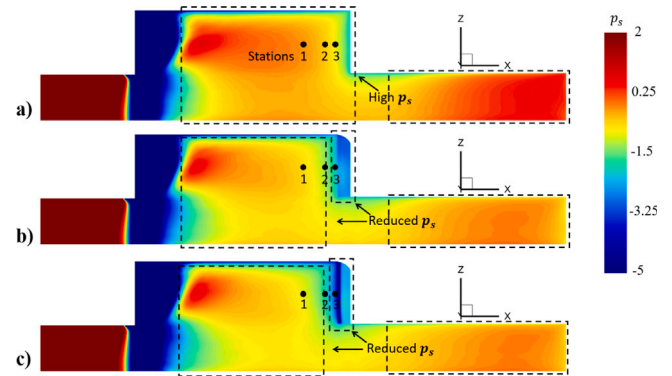


**Fig. 12.** Iso-surface of the time-averaged static pressure at  $p_s = -5$  Pa (blue) and  $-4$  Pa (gray) with vortex cores marked by white lines: (a) Case 1, (b) Case 2, (c) Case 3.



**Fig. 13.** The time-averaged static pressure contours at the starboard side (leeward) of CSM: (a) Case 1, (b) Case 2, (c) Case 3.

A question of interest is why the port-side TKE and  $\overline{u'v'}$  are suppressed by the current active flow control. For a detailed discussion, Fig. 20 plots the time-averaged  $u$ , TKE,  $\overline{u'v'}$ , and the gradient of  $u$  ( $\partial u/\partial y$ ) in the  $y$  (lateral) direction. These values are extracted from the three cases along the black dashed-dot lines in Station 2 (bottom row of Fig. 18), which cross the port-side high TKE region. Note that the data of  $\partial u/\partial y$  is post-processed by a Gaussian-weighted moving average filter



**Fig. 14.** The time-averaged static pressure contours at the port side (windward) of CSM: (a) Case 1, (b) Case 2, (c) Case 3.

using Matlab for more clear demonstration. As shown in the bottom of Fig. 20, the TKE of all three cases varies in the same pattern as their shear stresses  $\overline{u'v'}$ . The  $\overline{u'v'}$  first increases towards  $y/W = -0.4$  followed by a reduction towards  $y/W = -0.2$ , and so does TKE. This suggests that the TKE variation results from the shear stress variation, and the reduction in  $\overline{u'v'}$  leads to the suppression of TKE. Now, the question becomes why the port-side  $\overline{u'v'}$  is reduced in Case 3. The shear stress or the value of  $\overline{u'v'}$  indicates there is a  $u$  velocity gradient along the  $y$  direction, and the larger the velocity gradient (in magnitude), the higher the  $\overline{u'v'}$ , which are supported by the fact observed in Fig. 19 that high-shear-stress regions are located at the boundary between high and low speed regions. For the current case, the port-side  $\overline{u'v'}$  is caused by the low-speed cross-deck flow from starboard meeting with the high-speed port-side flow as demonstrated in Fig. 9(b), (e), and (h). With the AFC applied, the side-jet injected from the port-side slot in Case 3 not only suppresses low-speed region as shown in Figs. 16 and 19 but also serves as a buffer between the high and low speed flows as shown in Fig. 9(h), which all contribute to alleviating the velocity gradient. The alleviated velocity gradient can be observed in the  $\partial u/\partial y$  plot in Fig. 20, where Case 3 maintains the lowest magnitude of velocity gradient before the  $\overline{u'v'}$  and TKE reaches the maximum at  $y/W = -0.4$ . The  $u$  distribution shown on the top of Fig. 20 also demonstrates that the velocity of Case 3 drops in the mildest manner. Therefore, it is the alleviated velocity gradient achieved by the current AFC that suppresses  $\overline{u'v'}$  and TKE. Compared to the baseline Case 1, the maximum TKE and  $\overline{u'v'}$  in Case 3 are reduced by 15.0% and 37.2%, respectively.

#### 4. Applying the current AFC on a real ship

For the future application of the current AFC on a real ship, three issues are considered and discussed in this section. The first issue is the Reynolds number effect. The  $Re$  for a real ship will be much higher than the model's, but the flow structures will be similar. This is because the bluff bodies (including the ship model) can achieve the independence of  $Re$  when it is higher than  $2 \times 10^4$  (Sohankar, 2006; Lim et al., 2007), and the current study uses a  $Re$  of  $8 \times 10^4$ . Therefore, the effect of  $Re$  will not significantly affect the flow control results, and the conclusions acquired from the model should be the same as they are for a real ship.

The second issue is the implementation of the current AFC on a real ship. Apart from the base shape modifications (jet slots and Coanda surfaces) mentioned in the current paper, there are two more

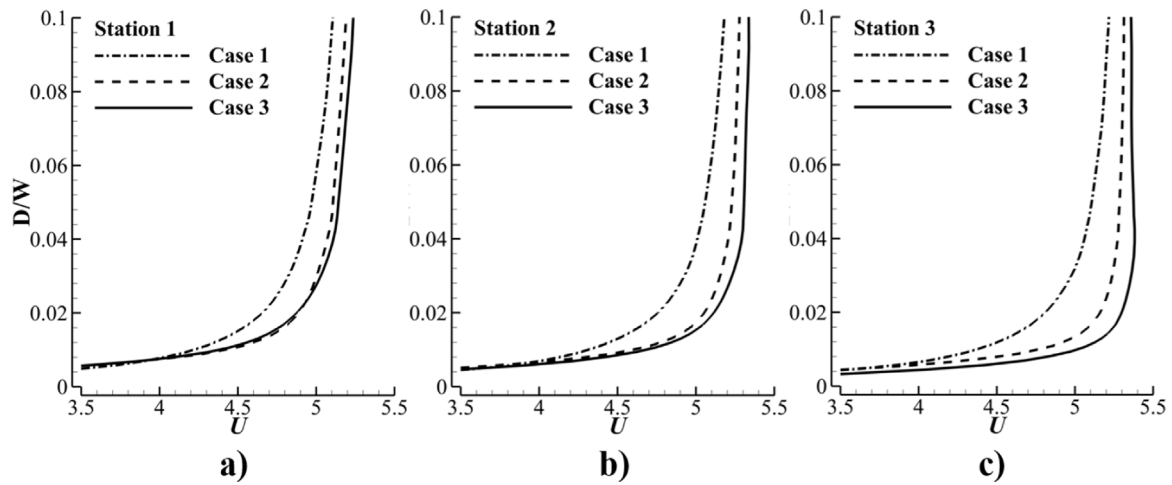


Fig. 15. The time-averaged  $u$  velocity profiles perpendicular to the port-side surface at: (a) Station 1, (b) Station 2, (c) Station 3; Location of stations is shown in Fig. 14.

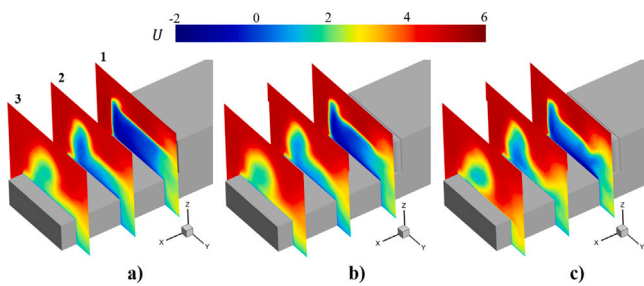


Fig. 16. The time-averaged  $u$  contours at different streamwise locations on deck: (a) Case 1, (b) Case 2, (c) Case 3.

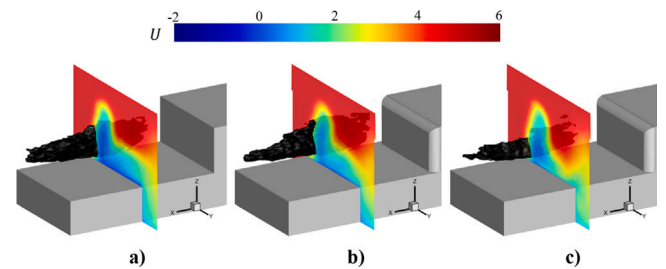


Fig. 19. The time-averaged  $u$  at Station 2 and iso-surface (black) of shear stress with  $u'v' = 0.03$ : (a) Case 1, (b) Case 2, (c) Case 3.

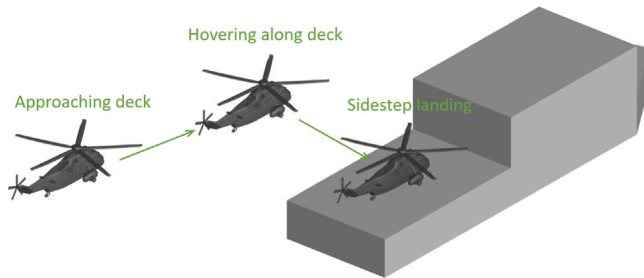


Fig. 17. Sketch of the helicopter recovery procedure, demonstrated using the Chalmers ship model.

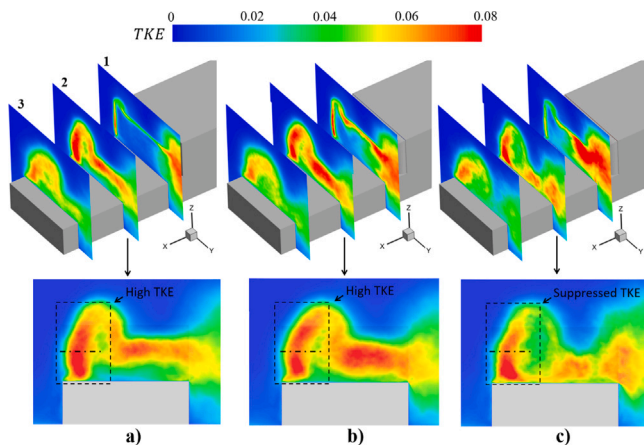


Fig. 18. Turbulent kinetic energy (TKE) contours at different streamwise locations on deck: (a) Case 1, (b) Case 2, (c) Case 3.

modifications that need to be made. The first one is to have a flow source as the AFC jet supply. This can be achieved by using a pressure tank or redirecting pressurized high-energy flow from the compressor of the ship's gas turbine engine. The second modification is to design a pipe or ducting system that connects flow sources to the injection slot with the minimum frictional loss.

The third one is to determine the proper slot size and  $C_\mu$  for a real ship. The injection slot size used here is normalized by the hanger height. When implementing the current AFC to a real ship, the actual slot size can be derived based on the real ship's hanger height. For the proper  $C_\mu$  to be effective, it can be achieved by constantly adjusting the  $C_\mu$  according to sailing environments and required control targets. Such control flexibility is also the major advantage of the current AFC method.

### 5. Conclusions

The present work studies the steady Coanda effect active flow control (AFC) for side force reduction and airwake manipulations under the yaw effect. The study is conducted numerically on the Chalmers ship model (CSM) using Large Eddy Simulation (LES) with Wall-Adapting Local-Eddy Viscosity (WALE) model. The AFC ship model is created by modifying the square-shaped hanger base to the Coanda surface with the addition of injection slots along the base's roof edge and two side edges. Three representative cases are studied for comparison: a baseline case, a no-jet case with the base modified to the Coanda surface, and an AFC case with jet blowing at a momentum coefficient ( $C_\mu$ ) of 0.02.

The results show that the base-shape modification significantly alters the vortex structure on deck from z-direction vortex (ZV) to streamwise vortex (SV), and the steady Coanda effect further enhances the SV with the removal of the port-side vortex (PV). As a result, the

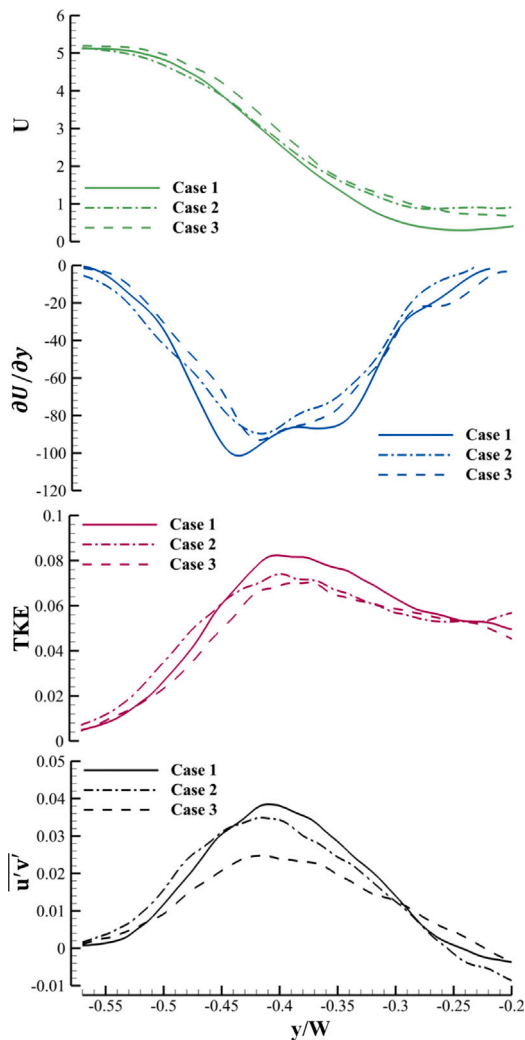


Fig. 20. Plots of the time-averaged  $u$ ,  $\partial u/\partial y$ , TKE, and  $\overline{u'v'}$  along  $y$  direction.

low-pressure region downstream of the base in the AFC case is more stretched with its distribution presenting a pronounced streamwise pattern. Due to the steady Coanda effect, the side force and yaw moment are mitigated by 5.27% and 7.97%, respectively, which can be attributed to the reduction of port-side (windward) surface static pressure. The steady Coanda effect can energize the flow on deck and reduce the areas of the low-speed region, especially on the starboard side. It is also found that the high-TKE (turbulent kinetic energy) region and high-shear-stress region along the port-side deck are significantly suppressed. Compared to the baseline case, the maximum TKE and  $\overline{u'v'}$  in the AFC case are reduced by 15.0% and 37.2%, respectively. This is because the jet blowing from the side slot serves as a buffer between the high-velocity main flow at the port and the low-velocity recirculating flow, which alleviates the velocity gradient and thus mitigates the shear layer and TKE.

The present work, for the first time, studies the performance of the steady Coanda effect AFC on a ship model at yaw. It is demonstrated that the current AFC works well with the selected yaw angle and significant advantages are achieved including drag and side-force reduction, streamwise velocity recovery in the near wake, and TKE and shear layer suppression, which are beneficial to the ship's maneuverability and maritime helicopter operations. For future study, the focus is expected to be on the larger and various yaw angles for evaluating the performance of the current AFC in more comprehensive wind conditions.

## CRediT authorship contribution statement

**Kewei Xu:** Conceptualization, Methodology, Software, Validation, Formal analysis, Investigation, Data Curation, Writing – original draft, Writing – review & editing, Visualization. **Xinchao Su:** Software, Investigation. **Yutao Xia:** Investigation. **Yitong Wu:** Investigation. **Rickard Bensow:** Validation, Writing – review & editing, Supervision, Project administration, Funding acquisition. **Sinisa Krajnovic:** Resources, Validation, Writing – review & editing, Supervision, Project administration, Funding acquisition.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

## Data availability

Data will be made available on request.

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